

## Quantum Machine Learning, TensorFlow and Edward



← Feynman  
quote

Talk by R.R.Tucci

## Quantum Toronto



PottersVille is allusion to famous American movie “It’s a Wonderful Life”

## Quantum Open Source

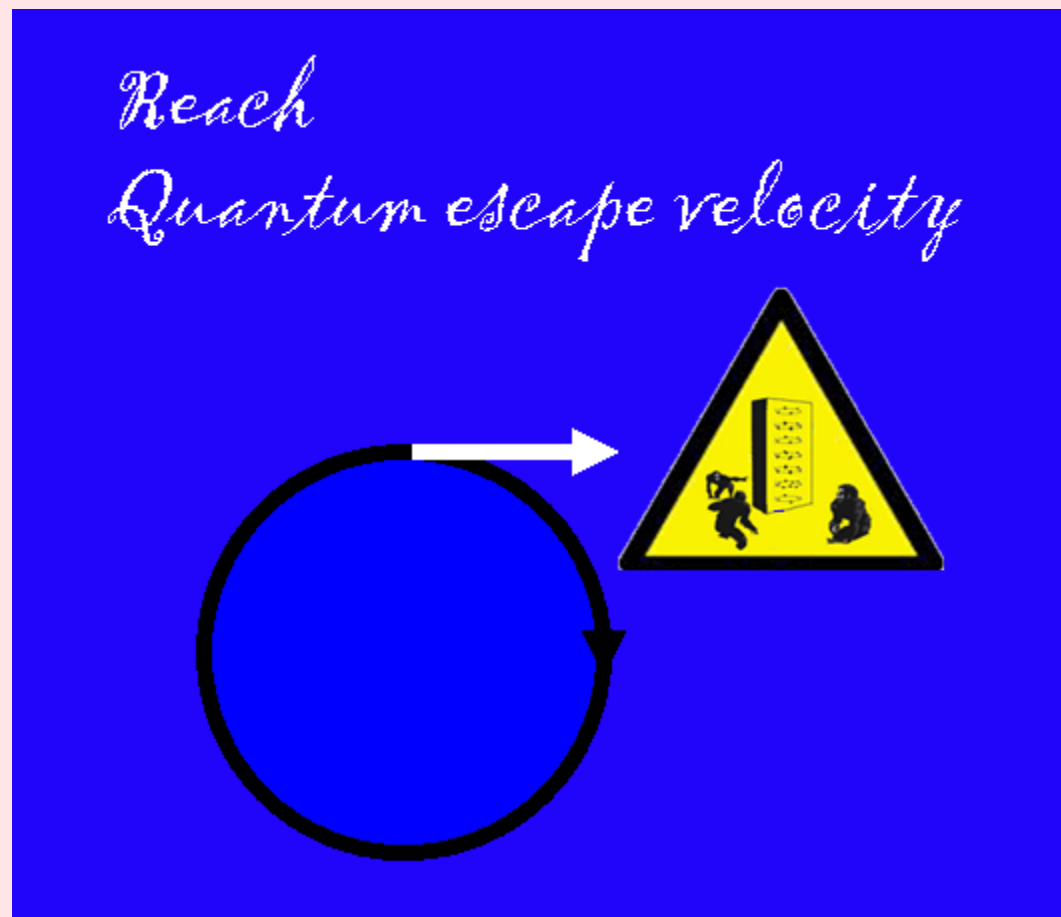


From  
Classic  
1984  
Apple adv.

## Quantum Ready



## Reach Quantum Escape Velocity (Quantum Supremacy)



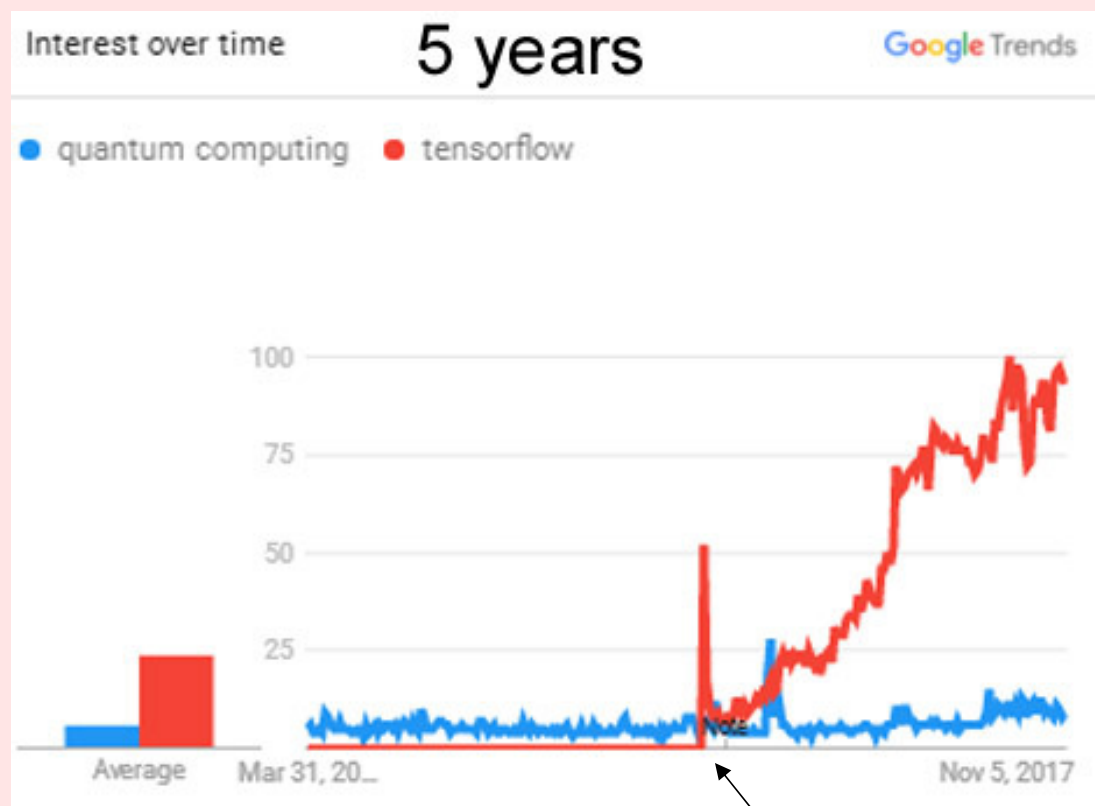
# What Does a Quantum Computer Look Like



Everything in this image except blue rings comes from tee-shirt sold on web



## Result of GoogleTrends search for keywords “TensorFlow” and “Quantum Computing”



TensorFlow Released as Open-Source

## Relationship between TensorFlow and Edward

Before Edward came along, TensorFlow could only do networks with deterministic nodes.

With the addition of Edward, TensorFlow now can do nets with both deterministic and non-deterministic (probabilistic) nodes.

The main author of Edward is Dustin Tran. He started writing Edward at Columbia Univ, as part of his Ph.D. thesis, under Prof. David Blei.

Edward is now officially a part of TensorFlow, and Dustin Tran now works for Google/TensorFlow.



# Pioneers mentioned in this talk

Judea Pearl, Bayesian Networks

Andrew Gelman, Hierarchical Models

Hierarchical Models \subset Bayesian Networks

Dustin Tran, Main Author of Edward Lib

David Blei, thesis advisor of Dustin,  
one of 3 authors of seminal paper for  
BBVI (Black Box Variational Inference)

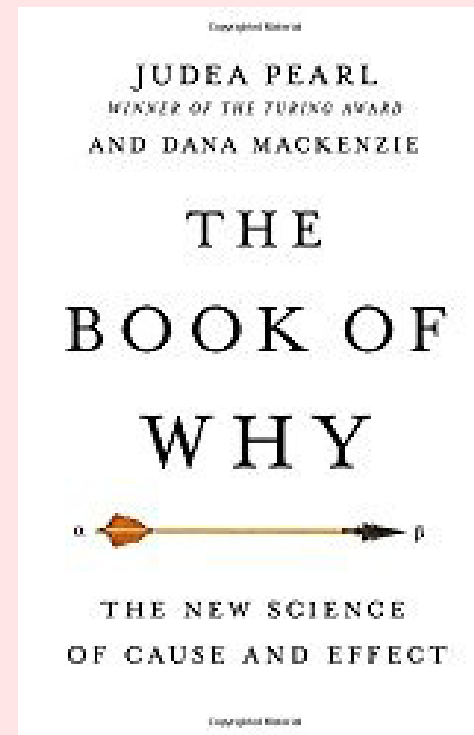
# Judea Pearl (UCLA)

Bayesian Networks, Causality.

Winner of Turing Prize in Computer Science

Wikipedia: [https://en.wikipedia.org/wiki/Judea\\_Pearl](https://en.wikipedia.org/wiki/Judea_Pearl)

Amazon Page: <https://www.amazon.com/Judea-Pearl/e/B001HCTYSO/>



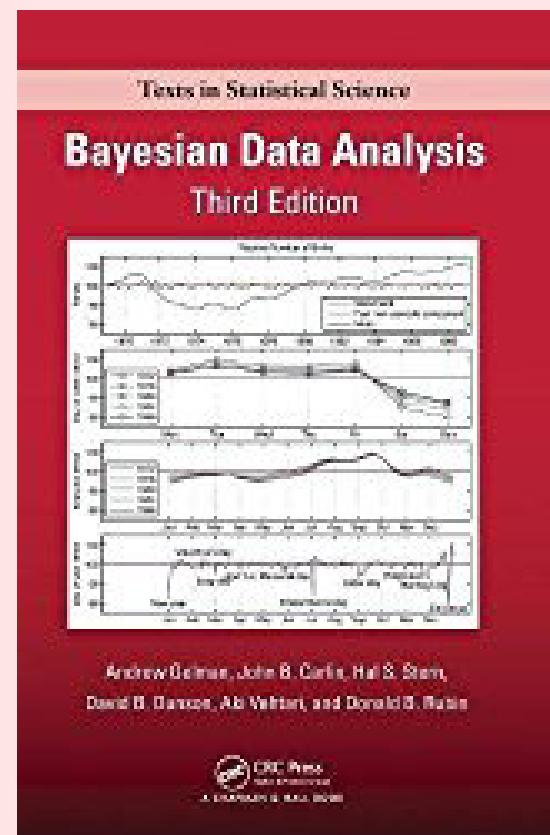
Just  
Published,  
May 2018

# Andrew Gelman (Columbia Univ)

## Hierarchical Models

Wikipedia: [en.wikipedia.org/wiki/Andrew\\_Gelman](https://en.wikipedia.org/wiki/Andrew_Gelman)

Amazon Page: <https://www.amazon.com/Andrew-Gelman/e/B001IGUSKM/>



## Edward Lib

Home: <http://edwardlib.org/>

Forum : <https://discourse.edwardlib.org/>

GitHub: <https://github.com/blei-lab/edward>



Dustin Tran

## Relationship between Edward and Quantum Machine Learning (1/2)

Classical Bayesian Networks → Quantum Bayesian Networks

Probability matrices attached to each node → Matrices of complex “amplitudes” attached to each node

Probability →  $|\text{Amplitude}|^2$

“Quantum Bayesian Nets”, by R.R. Tucci,  
<https://arxiv.org/abs/quant-ph/9706039>

“Factorization of Quantum Density Matrices According to Bayesian and Markov Networks”, by R.R. Tucci  
<https://arxiv.org/abs/quant-ph/0701201>

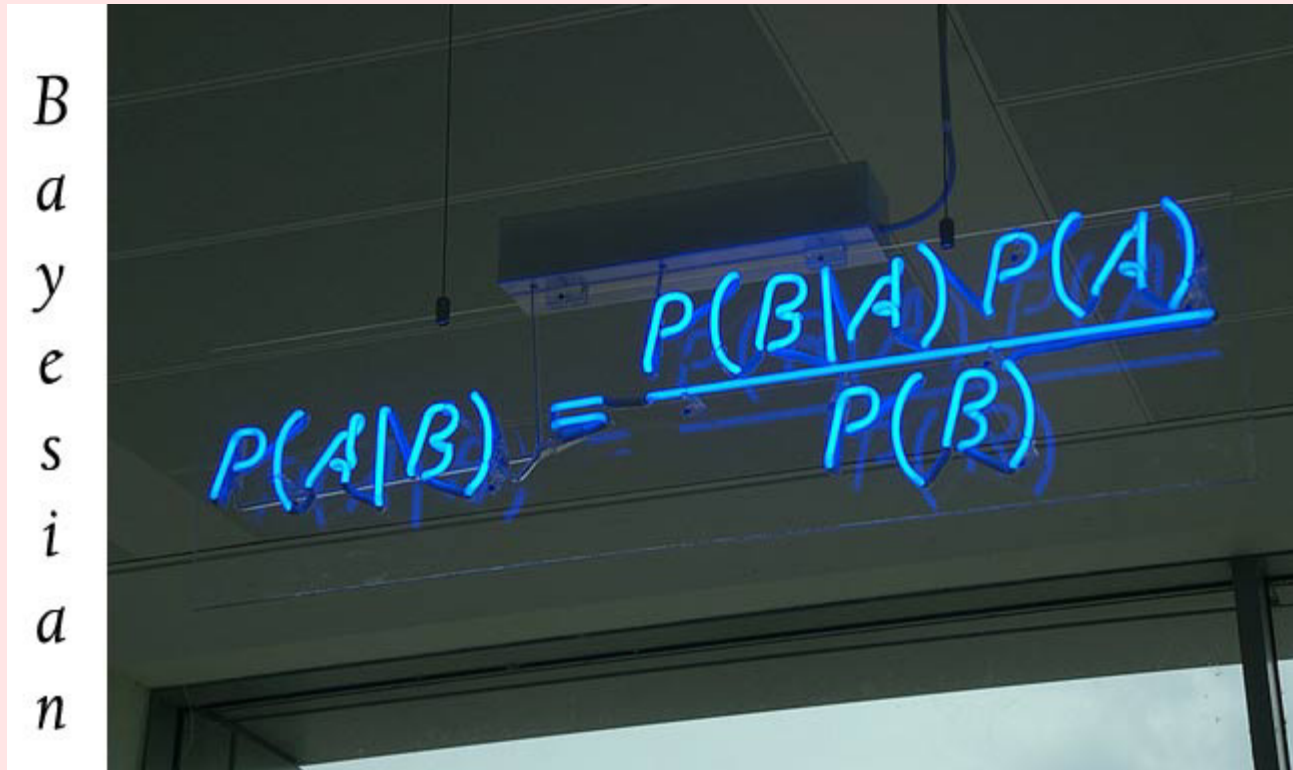
## Quantum



**“God does not play dice with the Universe”, A. Einstein  
Referring to Quantum Mechanics. God from Sistine Chapel**

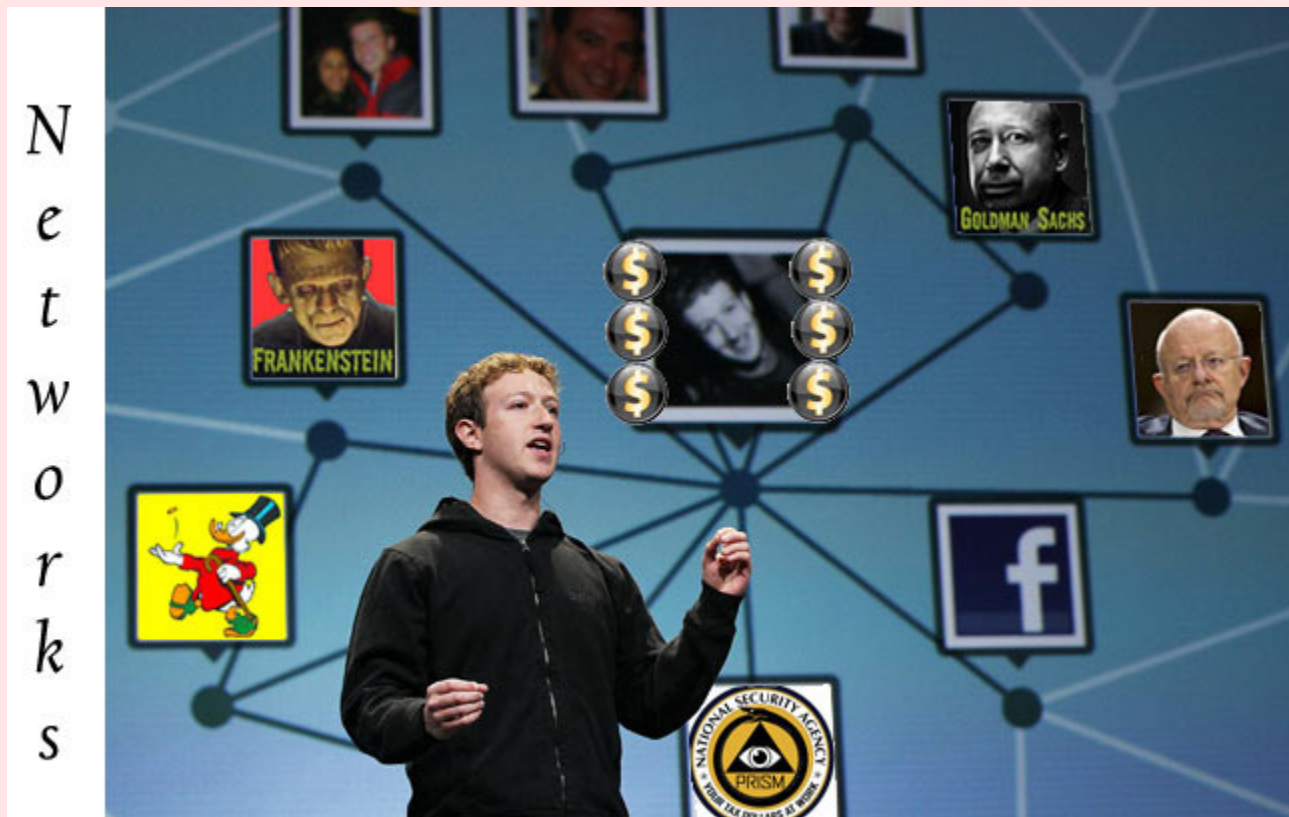


## Bayesian



Neon sign from Autonomy Corp. HQ in Cambridge, UK

## Networks



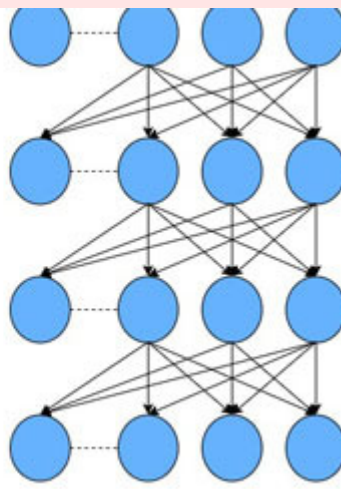
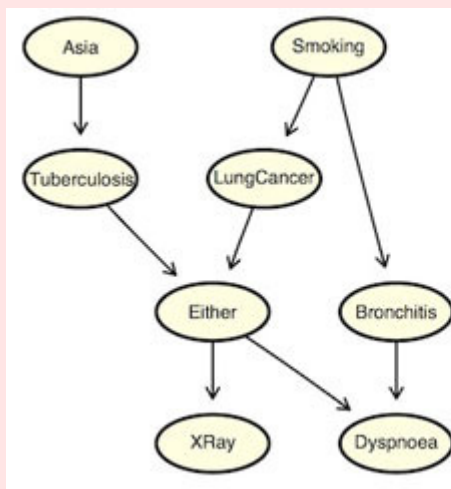
## Relationship between Edward and Quantum Machine Learning (2/2)

Edward → Quantum Edward

[https://github.com/artiste-qb-net/Quantum\\_Edward](https://github.com/artiste-qb-net/Quantum_Edward)

Quantum Edward at this point is just a small library of Python tools for doing classical supervised learning by Quantum Neural Networks (QNNs).

## TensorFlow Versus TensorLayer



Directed Acyclic Graphs,  
Bayesian Networks

Layers,  
Artificial Neural Networks

TensorFlow, Edward, PyMC

TensorLayer, PyTorch, Keras

**Classical**

Quantum Bayesian Networks

Quantum Circuits  
Qubiter

**Quantum**

Quantum Fog

Quantum Edward

## Quantum Edward (Prior & Future work)

An analytical model of a QNN is entered as input into QEdward and the training is done on a classical computer, using training data already available (e.g., MNIST), and using the famous BBVI (Black Box Variational Inference) method described in Reference 1 below. The BBVI method is a mainstay of the "Edward" software library.

This first version of Quantum Edward does not do distributed computing. The hope is that it can be used as a kindergarten to learn about these techniques, and that then the lessons learned can be used to write a library that does the same thing, classical supervised learning by QNNs, but in a distributed fashion using Edward/TensorFlow on the cloud.

### References

1. R. Ranganath, S. Gerrish, D. M. Blei, "Black Box Variational Inference", <https://arxiv.org/abs/1401.0118>

## Quantum Edward (Strategy)

The input analytical model of the QNN is given as a sequence of gate operations for a gate model quantum computer. The hidden variables are angles by which the qubits are rotated. The observed variables are the input and output of the quantum circuit. Since it is already expressed in the qc's native language, once the QNN has been trained using QEdward, it can be run immediately on a physical gate model qc such as the ones that IBM and Google have already built. By running the QNN on a qc and doing classification with it, we can compare the performance in classification tasks of QNNs and classical artificial neural nets (ANNs).



## Quantum Edward (Noisy Quantum Hardware)

Other workers have proposed training a QNN on an actual physical qc. But current qc's are still fairly quantum noisy. Training an analytical QNN on a classical computer might yield better results than training it on a qc because in the first strategy, the qc's quantum noise does not degrade the training.

## Quantum Edward (Two Examples)

The first version of Quantum Edward analyzes two QNN models called NbTrolsModel and NoNbTrolsModel. These two models were chosen because they are interesting to the author, but the author attempted to make the library general enough so that it can accommodate other akin models in the future. The allowable models are referred to as QNNs because they consist of 'layers', as do classical ANNs (Artificial Neural Nets). TensorFlow can analyze layered models (e.g., ANN) or more general DAG (directed acyclic graph) models (e.g., Bayesian networks).

# Quantum Edward, Docstring for class NbTrolsModel

[https://github.com/artiste-qb-net/Quantum\\_Edward/blob/master/NbTrolsModel.py](https://github.com/artiste-qb-net/Quantum_Edward/blob/master/NbTrolsModel.py)

## Docstring for class NbTrolsModel

### 1 / 4

```
class NbTrolsModel(Model):
    """
```

```
In this class and its twin class NoNbTrolsModel, we consider Quantum
circuits of the following kind. Below we represent them in Qubiter ASCII
picture notation in ZL convention, for nb=3 and na=4
```

```
[--nb---]  [----na-----]
```

```
NbTrols (nb Controls) model:
```

```
|0> |0> |0> |0> |0> |0> |0>
```

```
NOTA P(x) next
```

```
|---|---|---|---|---|---Ry
```

```
|---|---|---|---|---Ry--%
```

```
|---|---|---|---Ry--%---%
```

```
|---|---|---Ry--%---%---%
```

```
NOTA P(y|x) next
```

```
|---|---Ry--%---%---%---%
```

```
|---Ry--%---%---%---%---%
```

```
Ry--%---%---%---%---%---%
```

```
M   M   M
```

←P(q0)

←P(q1 | q0)

←P(q2 | q1, q0)

←P(q3 | q2, q1, q0)

x = (q3, q2, q1, q0)

←product = P(x)

←P(q4 | q3, q2, q1, q0)

←P(q5 | q4, q3, q2, q1, q0)

←P(q6 | q5, q4, q3, q2, q1, q0)

y = (q6, q5, q4)

←product = P(y | x)

Chain Rule for probabilities

## Docstring for class NbTrolsModel

2 / 4

```
NoNbTrols (no nb Controls) model:
```

```
|0> |0> |0> |0> |0> |0> |0>
```

```
NOTA P(x) next
```

```
|---|---|---|---|---|---Ry
```

```
|---|---|---|---|---Ry--%
```

```
|---|---|---|---Ry--%---%
```

```
|---|---|---Ry--%---%---%
```

```
NOTA P(y|x) next
```

```
|---|---Ry--%---%---%---%
```

```
|---Ry--|---%---%---%---%
```

```
Ry--|---|---%---%---%---%
```

```
M   M   M
```

A gate `|---|---Ry--%---%---%---%` is called an MP\_Y Multiplexor, or plexor for short. In Ref.1 (Qubiter repo at github), see Rosetta Stone pdf and Quantum CSD Compiler folder for more info about multiplexors.

In NbTrols and NoNbTrols models, each layer of a list1 corresponds to a single plexor. We list plexors (layers) in a list1 in order of increasing distance between the Ry target qubit and the 0th qubit.

## Docstring for class NbTrolsModel

### 3 / 4

Note that the expansion of a multiplexor into elementary gates (cnots and single qubit rotations) contains a huge number of gates (exp in the number of controls). However, such expansions can be shortened by approximating the multiplexors, using, for instance, the technique of Ref.2.

Ref.3 explains the motivation for choosing this model. This model is in fact guaranteed to fully parametrize  $P(\mathbf{x})$  and  $P(y|\mathbf{x})$ .

The circuits given above are for finding a fit of both  $P(\mathbf{x})$  and  $P(y|\mathbf{x})$ . However, if one wants to use a physical hardware device as a classifier, then one should omit the beginning part of the circuits (the parts that represent  $P(\mathbf{x})$ ), and feed the input  $\mathbf{x}$  into the first  $n_a$  qubits. In other words, for classifying, use the following circuits instead of the ones above:



## Docstring for class NbTrolsModel

4 / 4

```
[--nb---]  [-----na-----]
```

```
NbTrols (nb Controls) model:
```

```
|0> |0> |0>
```

```
|---|---Ry--%---%---%---%
```

```
|---Ry--%---%---%---%---%
```

```
Ry--%---%---%---%---%---%
```

```
M   M   M
```

```
NoNbTrols (no nb Controls) model:
```

```
|0> |0> |0>
```

```
|---|---Ry--%---%---%---%
```

```
|---Ry--|---%---%---%---%
```

```
Ry--|---|---%---%---%---%
```

```
M   M   M
```

```
References
```

```
-----
```

1. <https://github.com/artiste-qb-net/qubiter>

2. Oracular Approximation of Quantum Multiplexors and Diagonal Unitary Matrices, by Robert R. Tucci, <https://arxiv.org/abs/0901.3851>

3. Code Generator for Quantum Simulated Annealing, by Robert R. Tucci, <https://arxiv.org/abs/0908.1633> , Appendix B

4. "Quantum Edward Algebra.pdf", pdf included in this repo

## BBVI (Theory)

R. Ranganath, S. Gerrish, D. M. Blei, "Black Box Variational Inference", <https://arxiv.org/abs/1401.0118>

**BBVI uses ELBO maximization. Before reading the original BBVI paper, you might fortify yourself with the following background material from the Tutorials of the Edward home site:**

### **Variational Inference**

<http://edwardlib.org/tutorials/variational-inference>

### **KLqp minimization (same as ELBO maximization)**

<http://edwardlib.org/tutorials/klqp>

KL = Kullback Liebler, ELBO = Evidence Lower Bound

## BBVI (Long History)

[https://en.m.wikipedia.org/wiki/Variational\\_Bayesian\\_methods](https://en.m.wikipedia.org/wiki/Variational_Bayesian_methods)

Variational Inference: A Review for Statisticians

<https://arxiv.org/abs/1601.00670>

Berkeley Univ. Prof. Michael Jordan (same name as famous basketball player) was first to apply Variational Inference to Bayesian nets to do medical diagnosis.

Prof. M. Jordan was thesis advisor to David Blei, who became Prof. at Columbia Univ. Prof. D. Blei was thesis advisor to Dustin Tran. So BBVI spans at least 3 generations and + 20 years