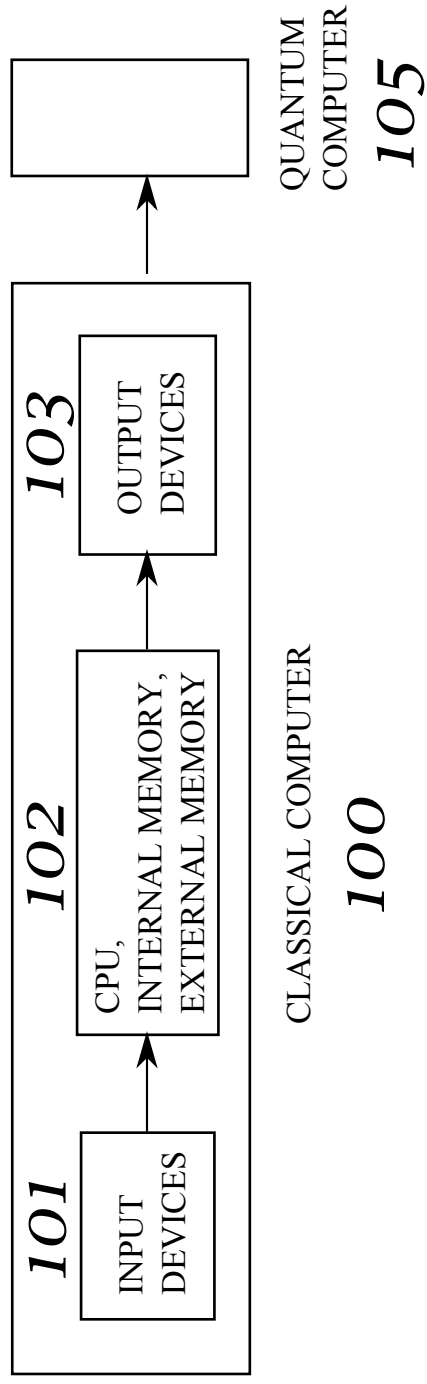


*Figure 1*



## *Figure 2*

$$|z_0|^2 + |z_1|^2 + \langle \chi | \chi \rangle = 1 \quad \mathbf{201}$$

$$p = |z_0|^2 + |z_1|^2, \quad q = 1 - p \quad \mathbf{202}$$

$$|s\rangle_{\mu,\nu,\omega} = \begin{array}{c} z_0 |\psi_0\rangle_\mu \\ |0\rangle_\nu \\ |0\rangle_\omega \end{array} + \begin{array}{c} z_1 |\psi_1\rangle_\mu \\ |1\rangle_\nu \\ |0\rangle_\omega \end{array} + \begin{array}{c} |\chi\rangle_{\mu,\nu} \\ |1\rangle_\omega \end{array} \quad \mathbf{203}$$

$$|t\rangle_{\mu,\nu,\omega} = \frac{1}{\sqrt{p}} \left[ \begin{array}{c} z_0 |\psi_0\rangle_\mu \\ |0\rangle_\nu \\ |0\rangle_\omega \end{array} + \begin{array}{c} z_1 |\psi_1\rangle_\mu \\ |1\rangle_\nu \\ |0\rangle_\omega \end{array} \right] \quad \mathbf{204}$$

$$\begin{aligned} [|t\rangle \langle t|]_{\mu,\nu,\omega} |s\rangle_{\mu,\nu,\omega} &= \sqrt{p} |t\rangle_{\mu,\nu,\omega} \\ [|0\rangle \langle 0|]_\omega |s\rangle_{\mu,\nu,\omega} &= \sqrt{p} |t\rangle_{\mu,\nu,\omega} \end{aligned} \quad \mathbf{205}$$

$$\begin{aligned} [|t\rangle \langle t|]_{\mu,\nu,\omega} |t\rangle_{\mu,\nu,\omega} &= |t\rangle_{\mu,\nu,\omega} \\ [|0\rangle \langle 0|]_\omega |t\rangle_{\mu,\nu,\omega} &= |t\rangle_{\mu,\nu,\omega} \end{aligned} \quad \mathbf{206}$$

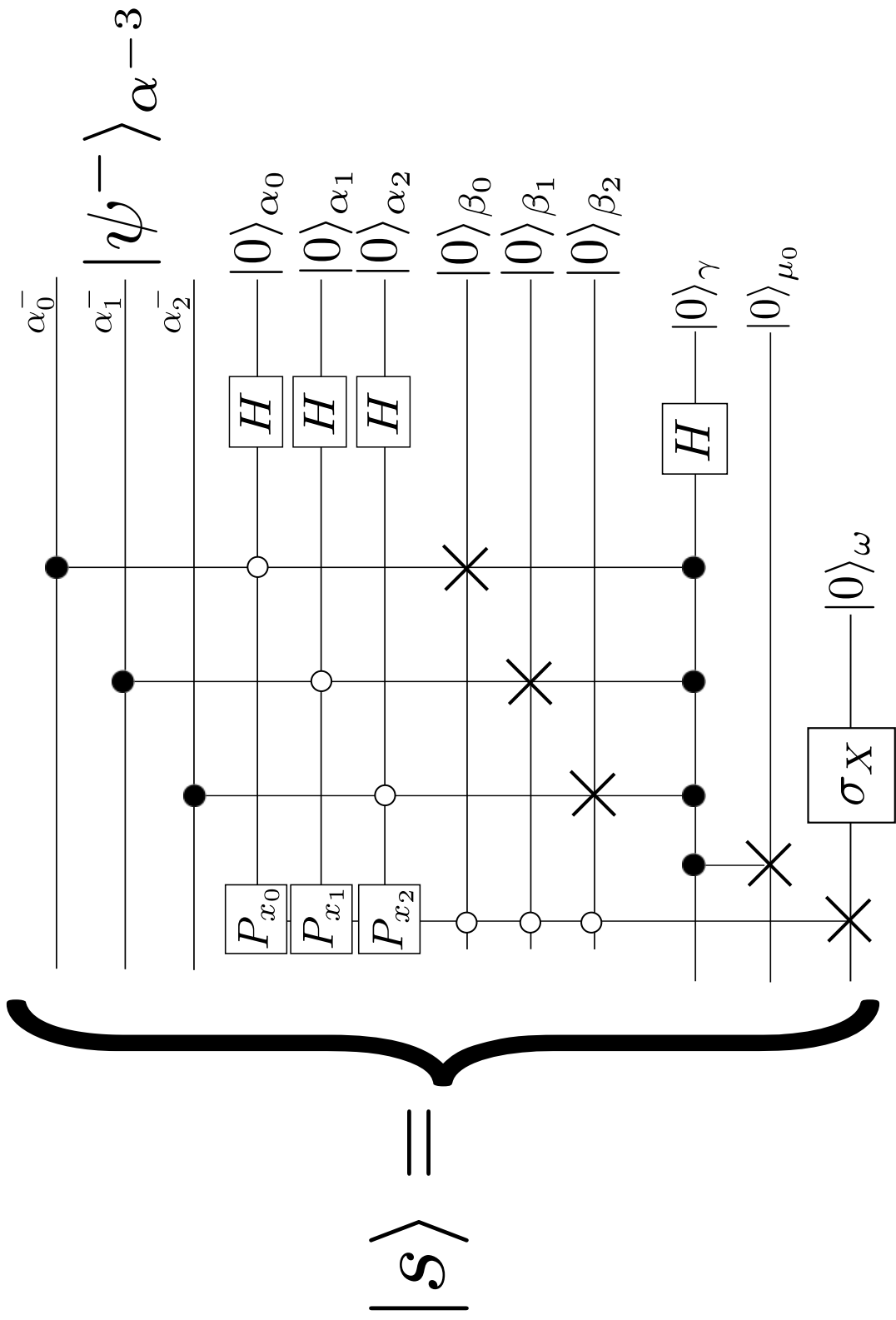
$$\langle t | s \rangle = \sqrt{p} \quad \mathbf{207}$$

$$\text{tr}_{\mu,\omega} \left\{ |t\rangle \langle t|_{\mu,\nu,\omega} \right\} = P(0) |0\rangle \langle 0|_\nu + P(1) |1\rangle \langle 1|_\nu \quad \mathbf{208}$$

$$P(0) = |z_0|^2/p, \quad P(1) = |z_1|^2/p \quad \mathbf{209}$$

$$|z_1|^2 = \frac{P(1)}{P(0)} |z_0|^2 \quad \mathbf{210}$$

Figure 3



# Figure 4

$$|s\rangle_{\mu,\nu,\omega} = \begin{matrix} z_1 |\psi_1\rangle_\mu \\ |1\rangle_\nu \\ |0\rangle_\omega \end{matrix} + \begin{matrix} z_0 |\psi_0\rangle_\mu \\ |0\rangle_\nu \\ |0\rangle_\omega \end{matrix} + \begin{matrix} |\chi\rangle_{\mu,\nu} \\ |1\rangle_\omega \end{matrix} \quad 401$$

$$|\psi_1\rangle_\mu = \frac{1}{\sqrt{f(x^3)}} \sum_{x^{-3}} \theta(x^3 \geq x^{-3}) A^-(x^{-3}) \begin{matrix} |x^{-3}\rangle_{\alpha^-} \\ |x^3\rangle_\alpha \\ |1\rangle_{\mu_0} \end{matrix}$$

$$|1\rangle_\nu = \begin{bmatrix} |0^3\rangle_\beta \\ |1\rangle_\gamma \end{bmatrix}$$

$$z_1 = \frac{1}{\sqrt{2^4}} \sqrt{f(x^3)}$$


$$\frac{|z_1|}{|z_0|} = \sqrt{\frac{P(1)}{P(0)}} \quad 405$$

$$|\psi_0\rangle_\mu = \begin{matrix} |\psi^-\rangle_{\alpha^-} \\ |x^3\rangle_\alpha \\ |0\rangle_{\mu_0} \end{matrix} \quad 402$$

$$|0\rangle_\nu = \begin{bmatrix} |0^3\rangle_\beta \\ |0\rangle_\gamma \end{bmatrix} \quad 403$$

$$z_0 = \frac{1}{\sqrt{2^4}} \quad 404$$

# Figure 5

***qMobius***   
(a "Mobius Resistor")

Ver. 1.6

**Inputs**

File Prefix

Number of  $|\psi\rangle$  qubits

**c vector**

bit 0

bit 1

bit 2

bit 3

Estimate of  $|z_1|^2 / |z_0|^2$

Maximum Number of Grover Steps

Gamma Tolerance (degs)

Delta Lambda (degs)

**Outputs**

$|z_0|^2$

Starting Gamma (degs)

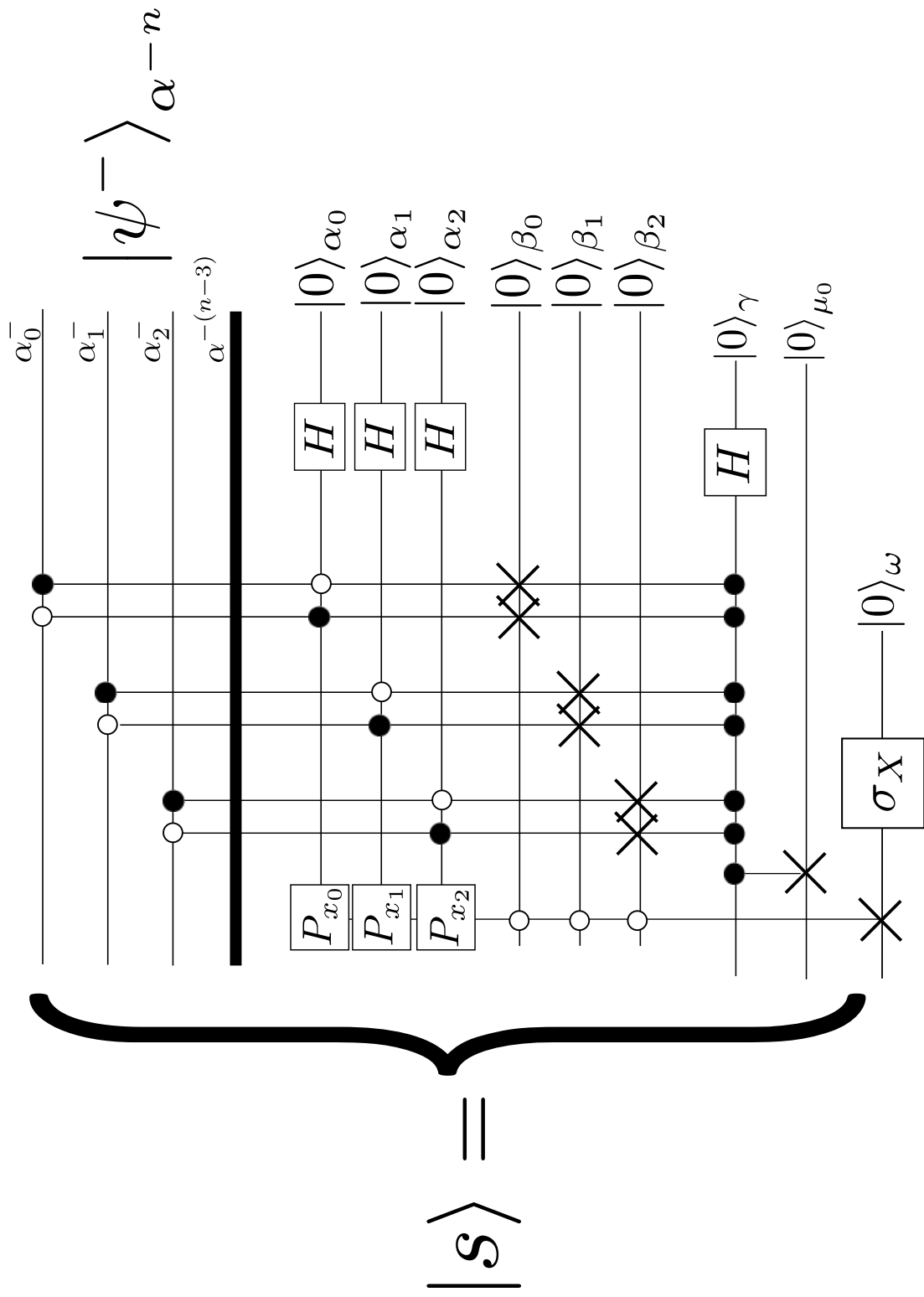
Final Gamma (degs)

Number of Grover Steps

Number of Qubits

Number of Elem. Ops.

Figure 6



# Figure 7

$$|s\rangle_{\mu,\nu,\omega} = \begin{matrix} z_1 |\psi_1\rangle_\mu \\ |1\rangle_\nu \\ |0\rangle_\omega \end{matrix} + \begin{matrix} z_0 |\psi_0\rangle_\mu \\ |0\rangle_\nu \\ |0\rangle_\omega \end{matrix} + \begin{matrix} |x\rangle_{\mu,\nu} \\ |1\rangle_\omega \end{matrix} \quad 701$$

$$|\psi_1\rangle_\mu = \frac{1}{\sqrt{P(x^3)}} \sum_{x^{-n}} \theta(x^3 = x^{-3}) A^-(x^{-n}) \begin{matrix} |x^{-n}\rangle_{\alpha^-} \\ |x^3\rangle_\alpha \\ |1\rangle_{\mu_0} \end{matrix}$$

$$|1\rangle_\nu = \left[ \begin{matrix} |0^3\rangle_\beta \\ |1\rangle_\gamma \end{matrix} \right]$$

$$z_1 = \frac{1}{\sqrt{2^4}} \sqrt{P(x^3)}$$

$$\frac{|z_1|}{|z_0|} = \sqrt{\frac{P(1)}{P(0)}} \quad 705$$

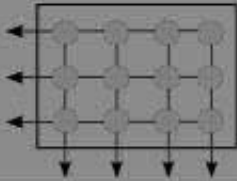
$$|\psi_0\rangle_\mu = \begin{matrix} |\psi^-\rangle_{\alpha^-} \\ |x^3\rangle_\alpha \\ |0\rangle_{\mu_0} \end{matrix} \quad 702$$

$$|0\rangle_\nu = \left[ \begin{matrix} |0^3\rangle_\beta \\ |0\rangle_\gamma \end{matrix} \right] \quad 703$$

$$z_0 = \frac{1}{\sqrt{2^4}} \quad 704$$

# Figure 8

*qMargi*



Ver. 1.6

**Inputs**

File Prefix

Number of  $|\psi\rangle$  qubits

Number of marginal qubits

**c vector**

bit 0

bit 1

bit 2

bit 3

Estimate of  $|z_1|^2 / |z_0|^2$

Maximum Number of Grover Steps

Gamma Tolerance (degs)

Delta Lambda (degs)

**Outputs**

$|z_0|^2$

Starting Gamma (degs)

Final Gamma (degs)

Number of Grover Steps

Number of Qubits

Number of Elem. Ops.